

# Fresnel Equations

- The fresnel effect is the observation that things get more reflective at grazing angles
- Fresnel equations describe how much energy is reflected at a surface boundary
- Remainder is absorbed as heat

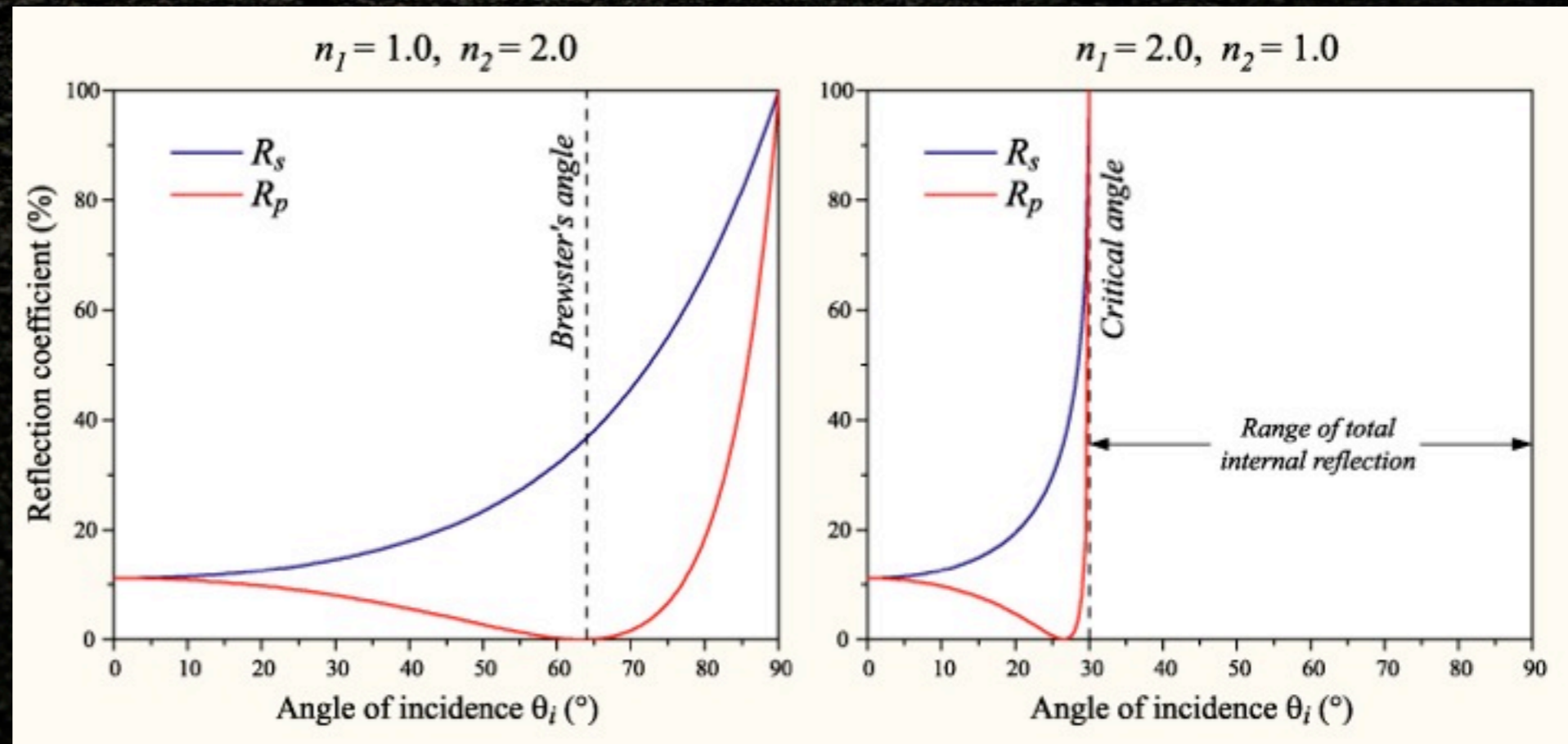
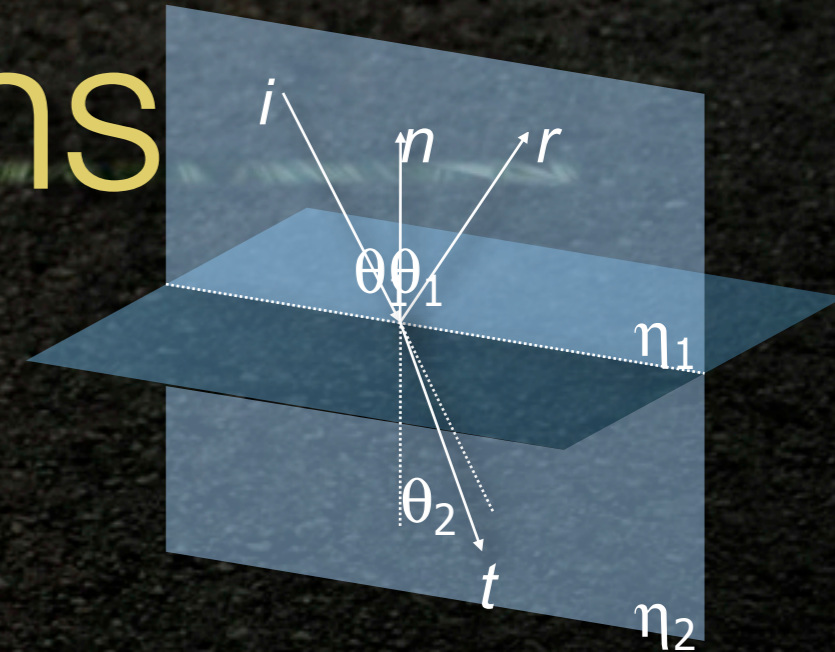


# Fresnel Equations

$$r_{\parallel}^2 = \frac{\sin^2(\theta_1 - \theta_2)}{\sin^2(\theta_1 + \theta_2)}$$

$$r_{\perp}^2 = \frac{\tan^2(\theta_1 - \theta_2)}{\tan^2(\theta_1 + \theta_2)}$$

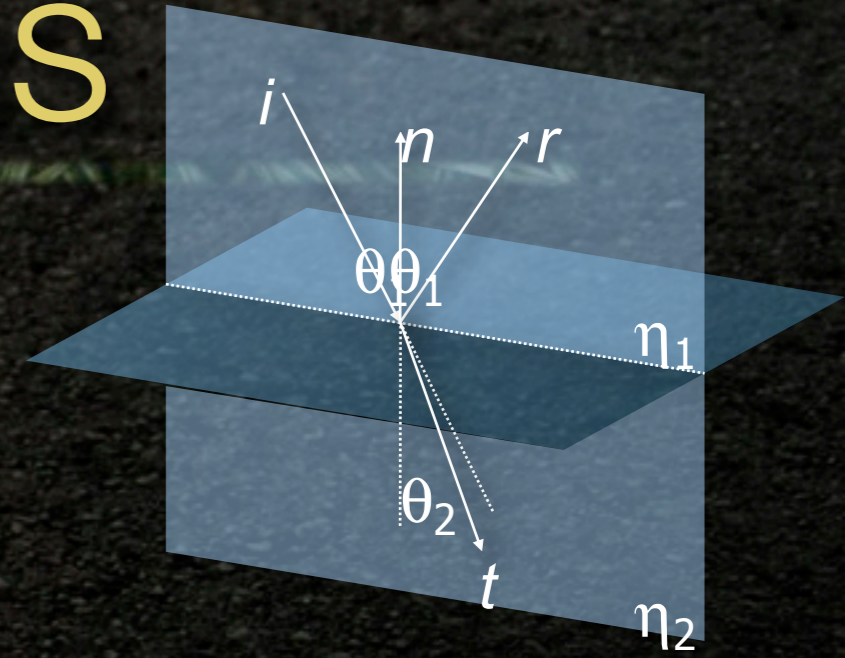
Fresnel equation for conductors





# Fresnel Equations

Fresnel equation for conductors



$$r_{\parallel}^2 = \frac{\sin^2(\theta_1 - \theta_2)}{\sin^2(\theta_1 + \theta_2)}$$

$$r_{\perp}^2 = \frac{\tan^2(\theta_1 - \theta_2)}{\tan^2(\theta_1 + \theta_2)}$$

$$F_r = \frac{1}{2}(r_{\parallel}^2 + r_{\perp}^2)$$



# Fresnel Equations

$$r_{\parallel}^2 = \frac{\sin^2(\theta_1 - \theta_2)}{\sin^2(\theta_1 + \theta_2)}$$

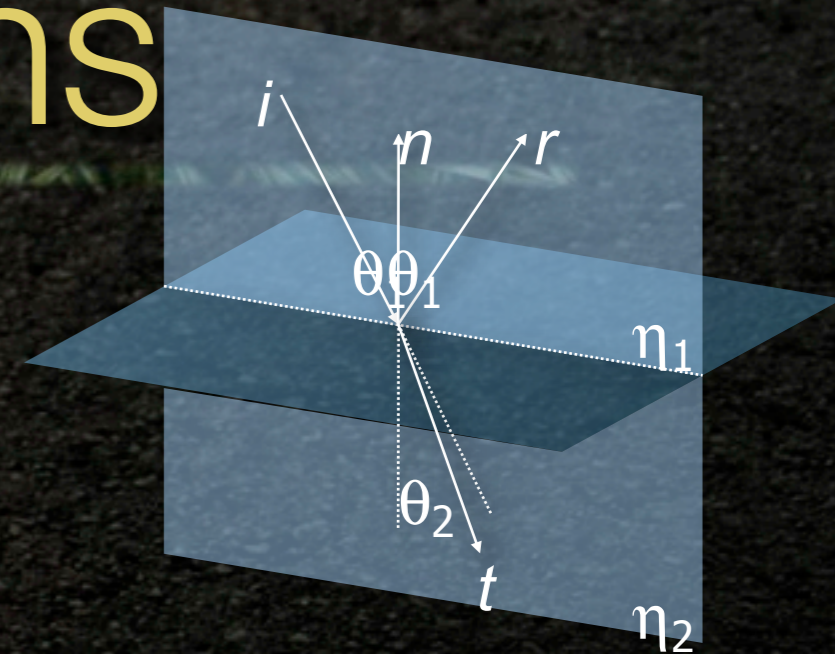
$$r_{\perp}^2 = \frac{\tan^2(\theta_1 - \theta_2)}{\tan^2(\theta_1 + \theta_2)}$$

$$F_r = \frac{1}{2}(r_{\parallel}^2 + r_{\perp}^2)$$

For  $\theta_1 = \theta_2 = 0$  :

$$F_r = \frac{(\eta_1 - \eta_2)^2}{(\eta_1 + \eta_2)^2}$$

$$\eta = \frac{1 + \sqrt{F_r}}{1 - \sqrt{F_r}}$$



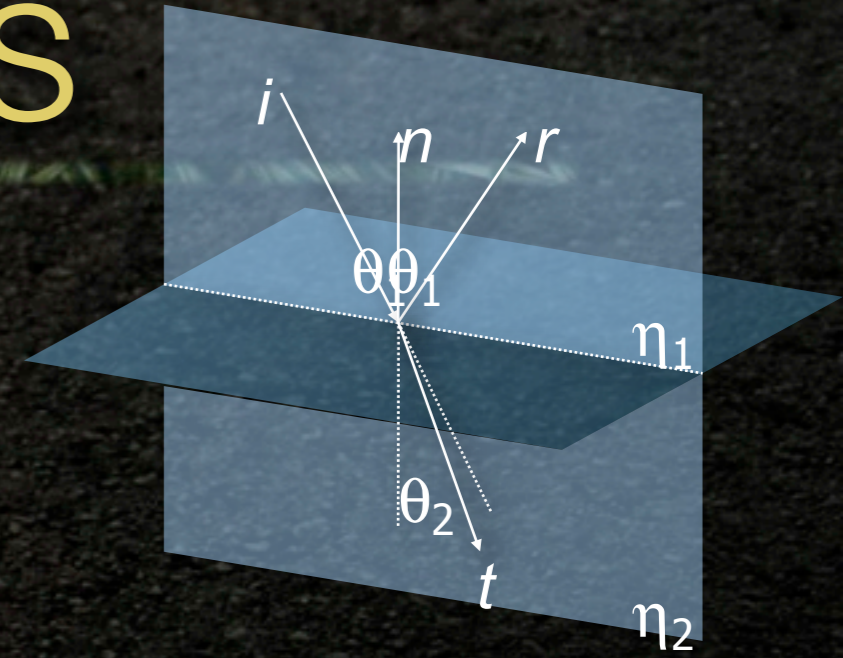


# Fresnel Equations

Schlick approximation:

$$F_r \approx R_0 + (1 - R_0)(1 - \cos \theta_1)^5$$

$$R_0 = \left( \frac{\eta - 1}{\eta + 1} \right)^2$$





# Metal shading

Compute hit position ( $\vec{P} = \vec{O} + t\vec{V}$ )

Call primitive to get normal ( $\vec{N}$ ) (normalized)

$$\text{costheta} = \vec{N} \cdot \vec{V}$$

if ( $\text{costheta} > 0$ )

    normal = -normal

else

    costheta = -costheta

foreach light source

    compute phong term, just like Phong material

result = speclight \*  $R_0$

if depth of ray < maximum depth:

$$F_r = R_0 + (1 - R_0)(1 - \text{costheta})^5$$

reflection direction =  $\vec{V} + 2\text{costheta}\vec{N}$

refl color = trace/shade ray(hitpos, reflection direction)

result +=  $F_r$  \* refl color



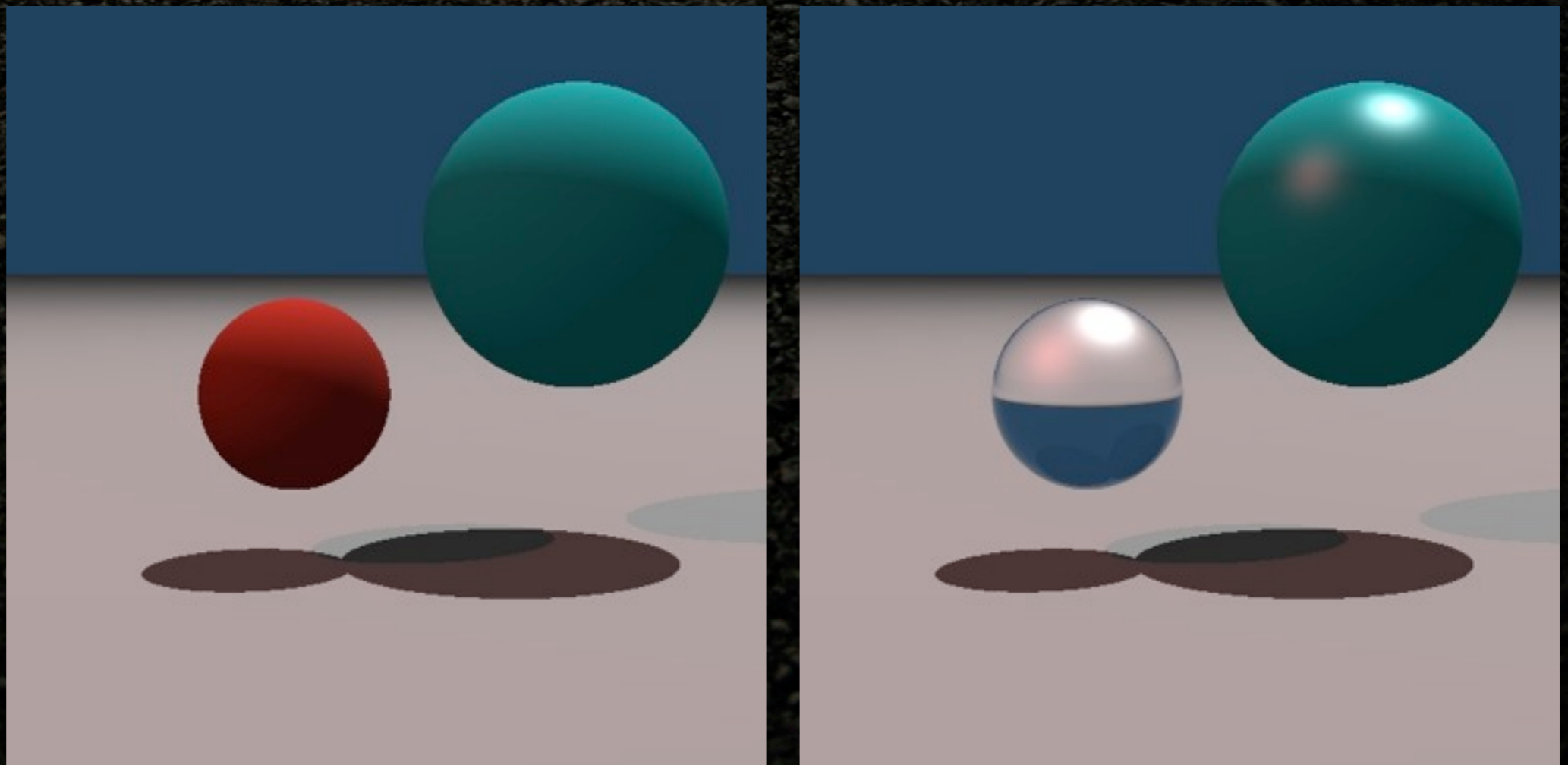
# Implementation tips

- Make sure the magnitude of your reflection direction == 1 (print it out)
- Scene now contains max ray depth
- Start with max ray depth==2



# Dielectric shading

	From light sources	From other surfaces
Diffuse reflection	-	-
Specular reflection	Phong term	Fresnel reflection
Diffuse transmission	-	-
Specular transmission	Phong term	Fresnel transmission





# Fresnel equations

Fresnel equations for transparency

$$r_{\parallel}^2 = \frac{\eta_2 \cos \theta_1 - \eta_1 \cos \theta_2}{\eta_2 \cos \theta_1 + \eta_1 \cos \theta_2}$$

$$r_{\perp}^2 = \frac{\eta_1 \cos \theta_1 - \eta_2 \cos \theta_2}{\eta_2 \cos \theta_2 + \eta_2 \cos \theta_2}$$

$$F_r = \frac{1}{2} (r_{\parallel}^2 + r_{\perp}^2)$$

$$F_t = 1 - F_r$$



# Fresnel Equations

$$r_{\parallel}^2 = \frac{\sin^2(\theta_1 - \theta_2)}{\sin^2(\theta_1 + \theta_2)}$$

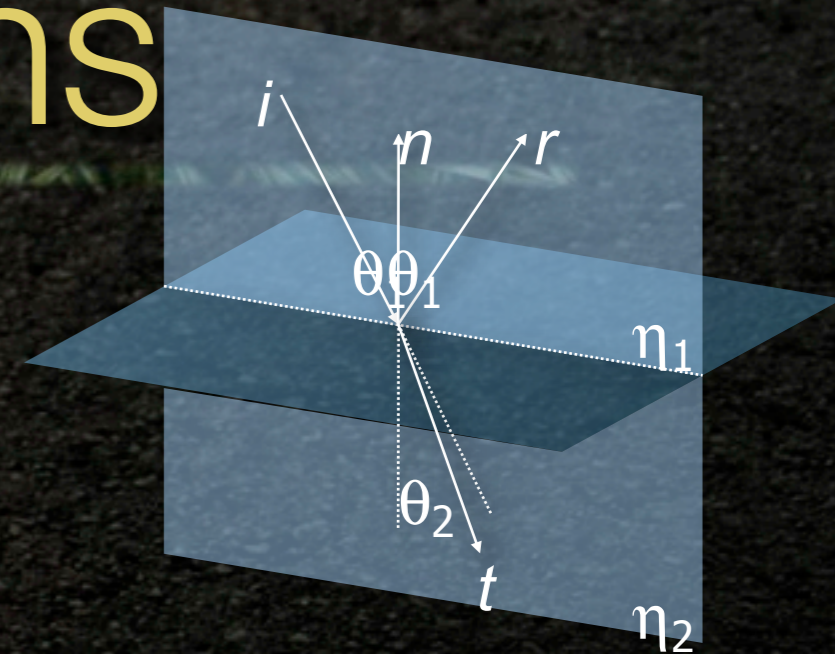
$$r_{\perp}^2 = \frac{\tan^2(\theta_1 - \theta_2)}{\tan^2(\theta_1 + \theta_2)}$$

$$F_r = \frac{1}{2}(r_{\parallel}^2 + r_{\perp}^2)$$

For  $\theta_1 = \theta_2 = 0$  :

$$F_r = \frac{(\eta_1 - \eta_2)^2}{(\eta_1 + \eta_2)^2}$$

$$\eta = \frac{1 + \sqrt{F_r}}{1 - \sqrt{F_r}}$$





# Fresnel Equations

Schlick approximation:

$$F_r \approx R_0 + (1 - R_0)(1 - \cos \theta_m)^5$$

$$\theta_m = \max(\theta_1, \theta_2)$$

$$F_t = 1 - F_r$$

$$R_0 = \left( \frac{\eta - 1}{\eta + 1} \right)^2$$

