

# Image Noise and Filtering

CS/BIOEN 4640: Image Processing Basics

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# Types of Image Noise

- ▶ Thermal Noise (additive Gaussian noise)
- ▶ Shot noise (random counts, Poisson noise)
- ▶ Salt-and-Pepper (replacement noise)
- ▶ Rician noise (magnitude of 2D Gaussian, MRI)

# Thermal Noise

- ▶ Thermal noise (or Johnson-Nyquist noise) is due to random fluctuations of electrons.
- ▶ When the signal from a photosensor is amplified, this noise is also amplified.
- ▶ “ISO level” controls the amount of amplification on digital cameras.
- ▶ Especially a problem in low-light situations – more amplification needed.
- ▶ Noise also gets worse with smaller sensor size and with denser packing of pixels.

# Thermal Noise as Additive Gaussian Noise

- ▶ Thermal noise is modeled as a Gaussian random value,  $\epsilon$ , added to the signal,  $s$ :

$$s' = s + \epsilon$$

- ▶ The random variable  $\epsilon$  has mean zero
- ▶ The random noise at each pixel is independent of other pixels
- ▶ The noise level ( $\sigma$  in Gaussian) is equal at all pixels

# Shot Noise

- ▶ Remember the photodiode signal strength is proportional to the number of photons that hit the sensor
- ▶ Photons hitting the sensor is a random process
- ▶ Shot noise is the noise due to this “counting” of a random number of photons
- ▶ Follows a Poisson distribution – can be approximated by a Gaussian

# Salt-and-Pepper Noise

- ▶ Also called “replacement” noise because some percentage of pixel values are just replaced by random numbers
- ▶ Example: “dead pixels” appear mostly dark due to defective sensor
- ▶ Example: “hot pixels” appear as overly bright pixels, due to charge leakage in long exposures

# Noise in Magnetic Resonance Imaging

- ▶ MRI is acquired in two channels
- ▶ Both channels are corrupted by additive Gaussian noise
- ▶ However, the image we view is the magnitude of the combined channels
- ▶ The resulting noise is Rice distributed
- ▶ It is not additive and not mean zero

# Filtering Additive Gaussian Noise

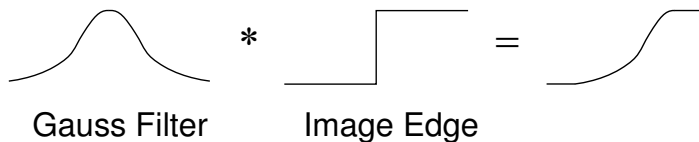
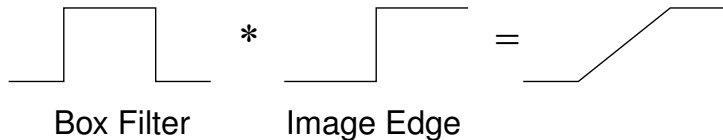
- ▶ White noise has mean zero.
- ▶ If we can average several pixels in a neighborhood with the same signal, the noise will “average out”:

$$E[s + \epsilon] = E[s] + E[\epsilon] = s$$

- ▶ Any filter that averages in a neighborhood will remove noise (e.g., box, gaussian)
- ▶ Of course, edges and textures are not constant, and these features also get blurred by averaging filters



# Comparison of Box vs Gaussian Filters



# Filtering Salt-and-Pepper Noise

- ▶ The noisy pixel is most likely an outlier, that is, looks much different from its neighbors
- ▶ Median filter does a good job of removing this
- ▶ Median will choose the middle of the distribution of neighbors
- ▶ Averaging does not work well because the outlier is included in the average (biasing the result up or down)