## Homework for Lecture 10, 11, 12

A liquid metal ( $\alpha$  phase) is contained in a container ( $\delta$  phase). Assume the melting point of the metal is  $T_m = 1350$  K, the molar entropy change of melting is  $\Delta S_M = S_L^0 - S_S^0 = 5.5$  J mol<sup>-1</sup> K<sup>-1</sup>, and the molar volume (for both the liquid and solid phase) is  $V_M = 9.6 \times 10^{-6}$  m<sup>3</sup>/mol. Now, we supercool the liquid metal to T = 1000 K,

1). What is the critical radius of homogeneous nucleation for solidification, if the interface energy between liquid ( $\alpha$ ) and solid ( $\beta$ ) phase,  $\gamma_{\alpha\beta} = 0.15 \text{ J/m}^2$ ?

2). If the interfacial energy between the liquid and the container is  $\gamma_{\alpha\delta} = 0.10 \text{ J/m}^2$  and that between the metal solid and the container is  $\gamma_{\beta\delta} = 0.175 \text{ J/m}^2$ , what is the contact angle of the heterogeneous nucleus on the container wall?

3). What is the volume of the critical heterogeneous nucleus on the container wall? Draw a schematic diagram of the nucleus on the container wall.